



BENCHMARKING OF I/O ACTIVITIES IN HPC APPLICATIONS WITH TRACE INSPECTOR

34TH POP WEBINAR | JUNE 2, 2025 | ARAVIND SANKARAN

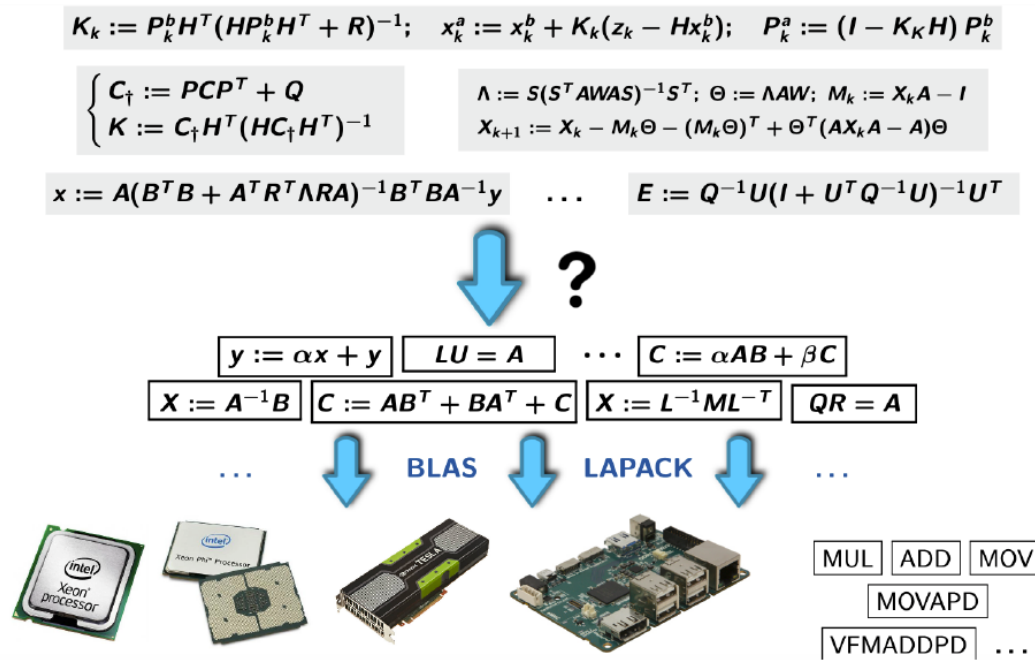
AGENDA

- About me
- The Story – Application benchmarks.
- Application Benchmarking with Directly-Follows-Graph (DFG).
- Synthesis of large amounts of I/O related system call traces.
- Final words.

THE LAMP STORY

The Linear Algebra Mapping Problem

The mapping of high level expressions to an optimized sequence of basic linear algebra operations.



THE LAMP STORY

The Linear Algebra Mapping Problem

Linear Algebra Expression

$$y := H^T y + (I_n - H^T H)x$$

where $H \in \mathbb{R}^{n \times n}$ $x, y \in \mathbb{R}^n$

Variant 1

$$y := H^T y + (I_n - H^T H)x$$

Operation	Kernel	FLOPs
$t_1 := H^T y$	gemv	$2n^2$
$T_2 := H^T H$	gemm	$2n^3$
$T_3 := I_n - T_2$	axpy	n
$t_4 := T_3 x$	gemv	$2n^2$
$y := t_1 + t_4$	axpy	n

$$\text{Total FLOPs} \approx 2n^3 + 4n^2 + 2n$$

Exec time $\approx 0.43\text{sec}$

Variant 2

$$y := H^T y + x - H^T(Hx)$$

Operation	Kernel	FLOPs
$t_1 := H^T y$	gemv	$2n^2$
$t_2 := Hx$	gemv	$2n^2$
$t_3 := H^T t_2$	gemv	$2n^2$
$t_4 := t_1 - t_3$	axpy	n
$y := t_4 + x$	axpy	n

$$\text{Total FLOPs} \approx 6n^2 + 2n$$

Exec time $\approx 0.003\text{sec}$

$$y := \alpha x + y \quad LU = A \quad \dots \quad C := \alpha AB + \beta C$$

$$X := A^{-1}B \quad C := AB^T + BA^T + C \quad X := L^{-1}ML^{-T} \quad QR = A$$

... BLAS LAPACK ...



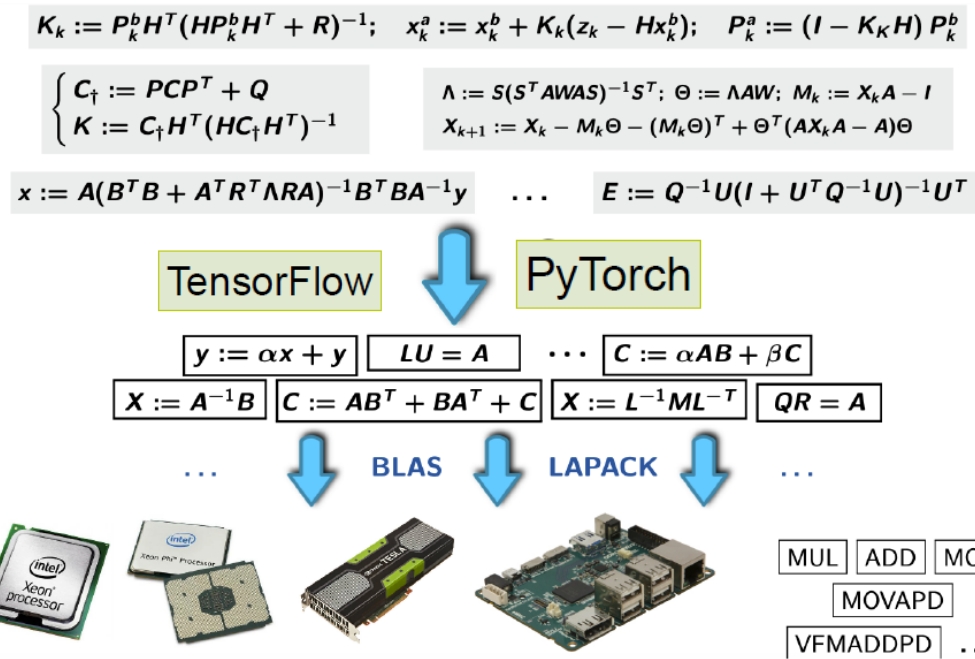
MUL ADD MOV
MOVAPD
VFMADDPD ...

Variant 2 is orders of magnitude faster than Variant 1!

THE LAMP STORY

The Linear Algebra Mapping Problem

The mapping of high level expressions to an optimized sequence of basic linear algebra operations.



Kernels are highly optimized.

THE LAMP STORY

The Linear Algebra Mapping Problem

The mapping of high level expressions to an optimized sequence of basic linear algebra operations.

$$K_k := P_k^b H^T (H P_k^b H^T + R)^{-1}; \quad x_k^a := x_k^b + K_k (z_k - H x_k^b); \quad P_k^a := (I - K_k H) P_k^b$$

$$\begin{cases} C_{\dagger} := P C P^T + Q \\ K := C_{\dagger} H^T (H C_{\dagger} H^T)^{-1} \end{cases}$$

$$\begin{aligned} \Lambda &:= S(S^T A W A S)^{-1} S^T; \quad \Theta := \Lambda A W; \quad M_k := X_k A - I \\ X_{k+1} &:= X_k - M_k \Theta - (M_k \Theta)^T + \Theta^T (A X_k A - A) \Theta \end{aligned}$$

$$x := A(B^T B + A^T R^T \Lambda R A)^{-1} B^T B A^{-1} y \quad \dots \quad E := Q^{-1} U (I + U^T Q^{-1} U)^{-1} U^T$$

Does the mapping make best use of the available kernels?

TensorFlow

PyTorch

$$\begin{aligned} & y := \alpha x + y \quad LU = A \quad \dots \quad C := \alpha AB + \beta C \\ & X := A^{-1} B \quad C := AB^T + BA^T + C \quad X := L^{-1} M L^{-T} \quad QR = A \end{aligned}$$

... BLAS LAPACK ...



MUL ADD MOV
MOVAPD
VFMADDPD ...

Kernels are highly optimized.

THE LAAB STORY

The Linear Algebra **Aware** Benchmarks

- Developed benchmarks to evaluate the linear algebra awareness of the build of popular ML framework (v2022).
- Designed to run in a continuous benchmarking setup to automatically generate reports (v2025 – yet to release).
- Source code: <https://github.com/HPAC/LAAB-Python>

Sample CB report

LAAB-Python | LA Awareness-CPU | PyTorch/2.1.2-foss-2023a | HPC2N_x86_64

This report evaluates whether the software build performs operations equivalent to those of optimized math libraries (e.g., OpenBLAS, MKL), and whether it leverages linear algebra techniques to accelerate CPU computations. Unless stated otherwise, all benchmarks use matrices of size 3000 × 3000 and are executed on a single CPU core of AMD EPYC 7413 24-Core Processor.

1) PyTorch vs. BLAS for matrix multiplication:

	Call	time (s)
$A^T B$	<code>t(A)@B</code>	0.5094 ✓
"	<code>linalg.matmul(t(A),B)</code>	0.5072 ✓
Reference	<code>sgemm</code>	0.4942

2) Elimination of common sub-expression:

$$E = A^T B + A^T B.$$

Expr	Call	time (s)
E	<code>t(A)@B + t(A)@B</code>	0.5251 ✓
Reference	<code>2*(t(A)@B)</code>	0.5271

$$E_1 = (A^T B)^T (A^T B) \text{ and } E_2 = (A^T B)^T A^T B.$$

Expr	Call	time (s)
E_1	<code>t(t(A)@B)@t(A)@B</code>	1.0191 ✓
E_2	<code>t(t(A)@B)@t(A)@B</code>	1.5224 ✗
Reference	<code>S=t(A)@B; t(S)@S</code>	1.0188

THE LAAB STORY

The Linear Algebra **Aware Benchmarks**

Sample CB report

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3) Choosing the optimal order to evaluate a matrix chain:

Given m matrices of suitable sizes, the product $M = A_1 A_2 \dots A_n$ is known as a matrix chain. Because of associativity of matrix product, matrix chain can be computed in many different ways, each identified by a specific paranthesization. The paranthesization that evaluates M with the least number of floating point operations (FLOPs) is considered optimal. PyTorch provides the method `torch.linalg.multi_dot` specifically for evaluation of matrix chains.

a) Right to left:

The input matrix chain is $H^T H x$, where x is a vector of lenth 3000. The reference implementation, evaluating from right-to-left - i.e., $H^T(Hx)$, avoids the expensive $O(n^3)$ matrix product, and has a complexity of $O(n^2)$.

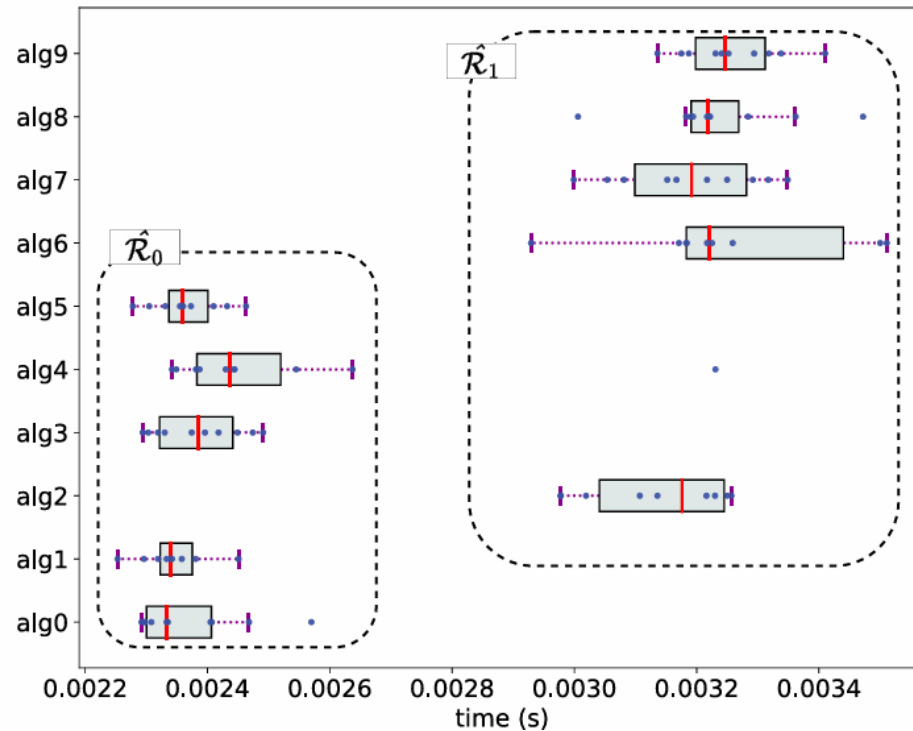
Expr	Call	time (s)
$H^T H x$	<code>t(H)@H@x</code>	0.5100 ✖
"	<code>linalg.multi_dot([t(H), H, x])</code>	0.0064 ✔
Reference	<code>t(H)@(H@x)</code>	0.0054

For more info, refer: A. Sankaran, N. A. Alashti, C. Psarras and P. Bientinesi, "Benchmarking the Linear Algebra Awareness of TensorFlow and PyTorch," 2022 *IEEE International Parallel and Distributed Processing Symposium Workshops (IPDPSW)*, Lyon, France, 2022, pp. 924-933, doi: 10.1109/IPDPSW55747.2022.00150.

BENCHMARKING WITH DFG

The algorithms use case

Identification of root causes of performance differences among algorithm variants.

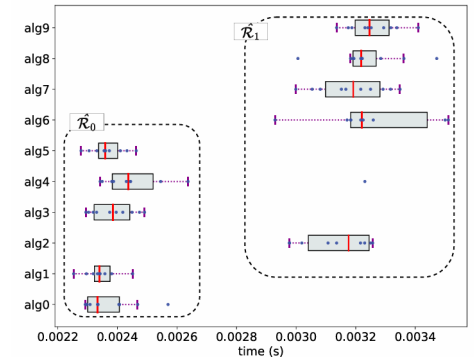
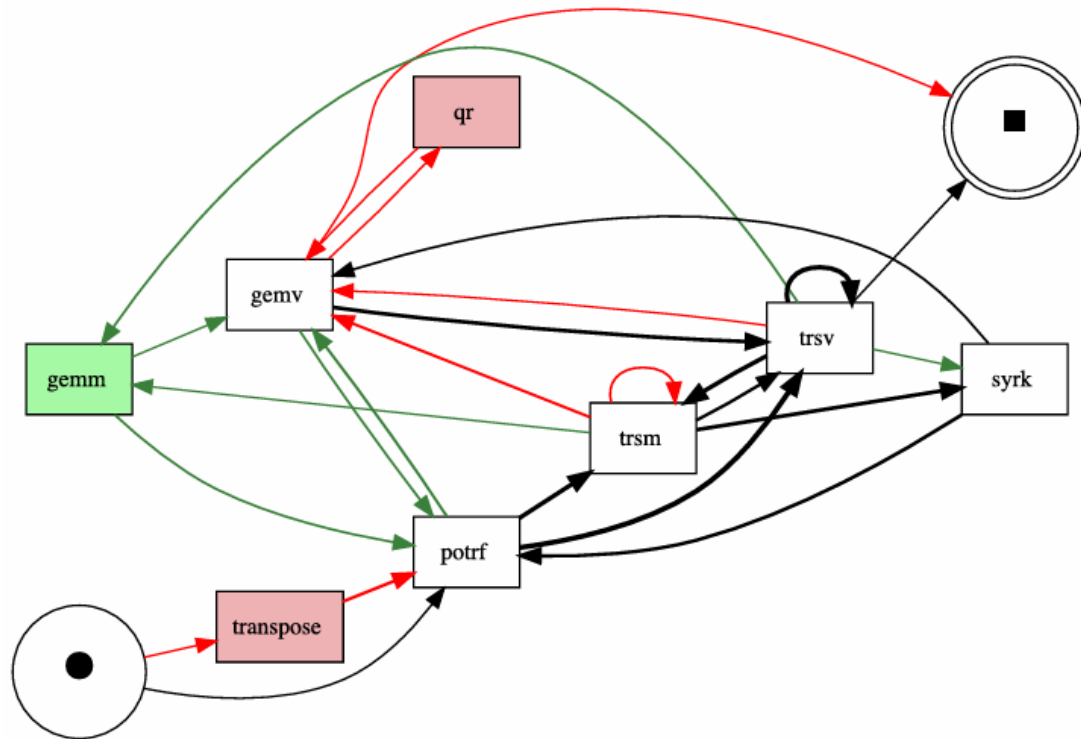


Variant	Kernel sequence
alg₀	potrf, trsm, trsv, syrk, gemv, potrf, trsv, trsv
alg₁	potrf, trsv, trsm, syrk, potrf, gemv, trsv, trsv
alg₂	potrf, trsm, trsv, syrk, gemv, qr, gemv, trsv
alg₃	potrf, trsv, trsm, gemm, potrf, gemv, trsv, trsv
alg₄	potrf, trsm, trsv, gemm, gemv, potrf, trsv, trsv
alg₅	potrf, trsm, trsv, gemm, potrf, gemv, trsv, trsv
alg₆	transpose, potrf, trsm, trsv, syrk, potrf, trsv, trsm, gemv, trsv
alg₇	transpose, potrf, trsm, syrk, potrf, trsv, trsv, trsm, gemv, trsv
alg₈	transpose, potrf, trsm, syrk, potrf, trsm, trsm, trsv, trsv, gemv
alg₉	transpose, potrf, trsm, syrk, potrf, trsv, trsv, trsm, trsm, gemv

Algorithmic variants of the generalized least square problem.

BENCHMARKING WITH DFG

The algorithms use case



Variant	Kernel sequence
alg₀	potrf, trsm, trsv, syrk, gemv, potrf, trsv, trsv
alg₁	potrf, trsv, trsm, syrk, potrf, gemv, trsv, trsv
alg₂	potrf, trsm, trsv, syrk, gemv, qr, gemv, trsv
alg₃	potrf, trsv, trsm, gemm, potrf, gemv, trsv, trsv
alg₄	potrf, trsm, trsv, gemm, gemv, potrf, trsv, trsv
alg₅	potrf, trsm, trsv, gemm, potrf, gemv, trsv, trsv
alg₆	transpose, potrf, trsm, trsv, syrk, potrf, trsv, trsm, gemv, trsv
alg₇	transpose, potrf, trsm, syrk, potrf, trsv, trsv, trsm, gemv, trsv
alg₈	transpose, potrf, trsm, syrk, potrf, trsm, trsm, trsv, trsv, gemv
alg₉	transpose, potrf, trsm, syrk, potrf, trsv, trsv, trsm, trsm, gemv

Ref: Sankaran, A., Karlsson, L. & Bientinesi, P. Ranking with ties based on noisy performance data. *Int J Data Sci Anal* (2025).
<https://doi.org/10.1007/s41060-025-00722-1>

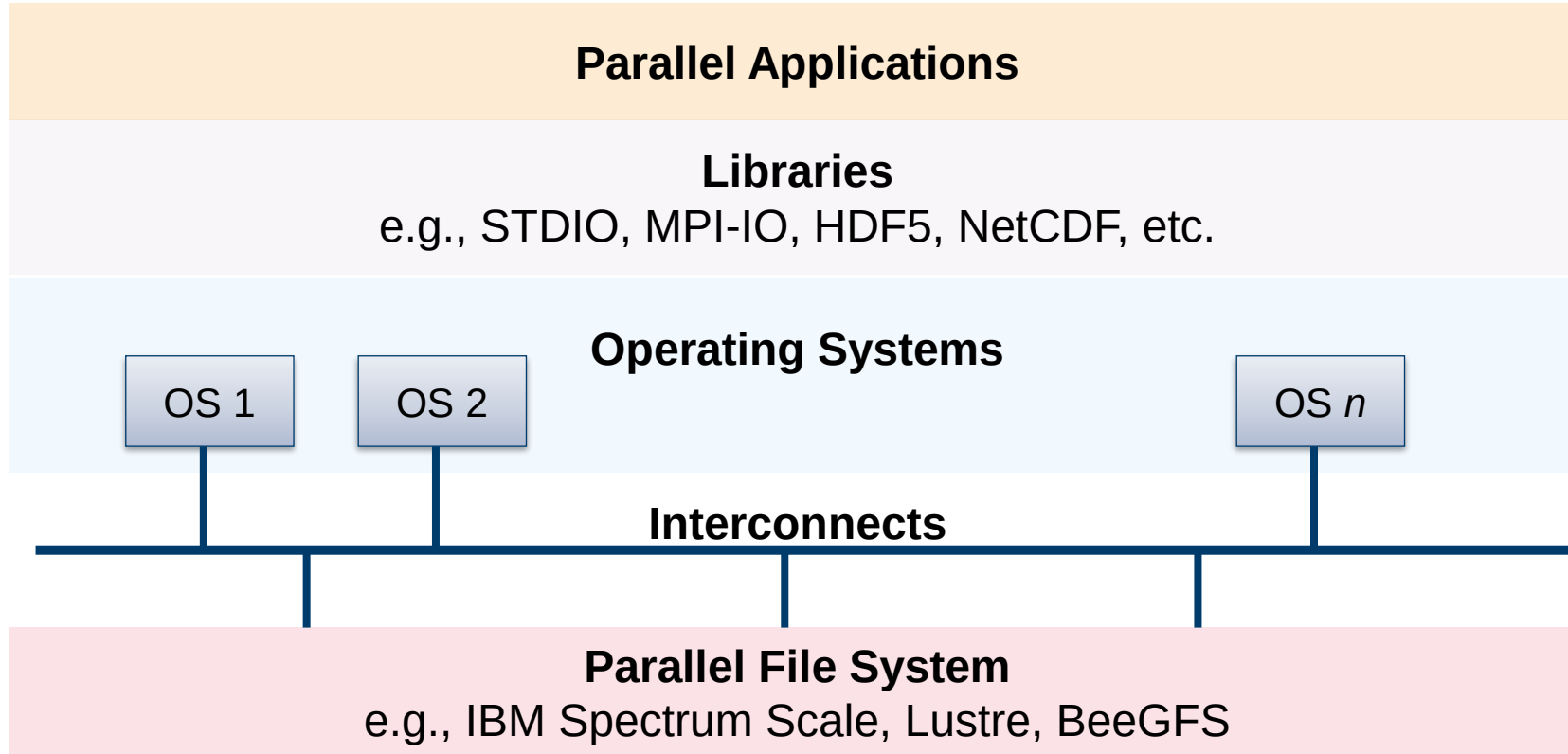
AND NOW,

The picture is incomplete without I/O information.

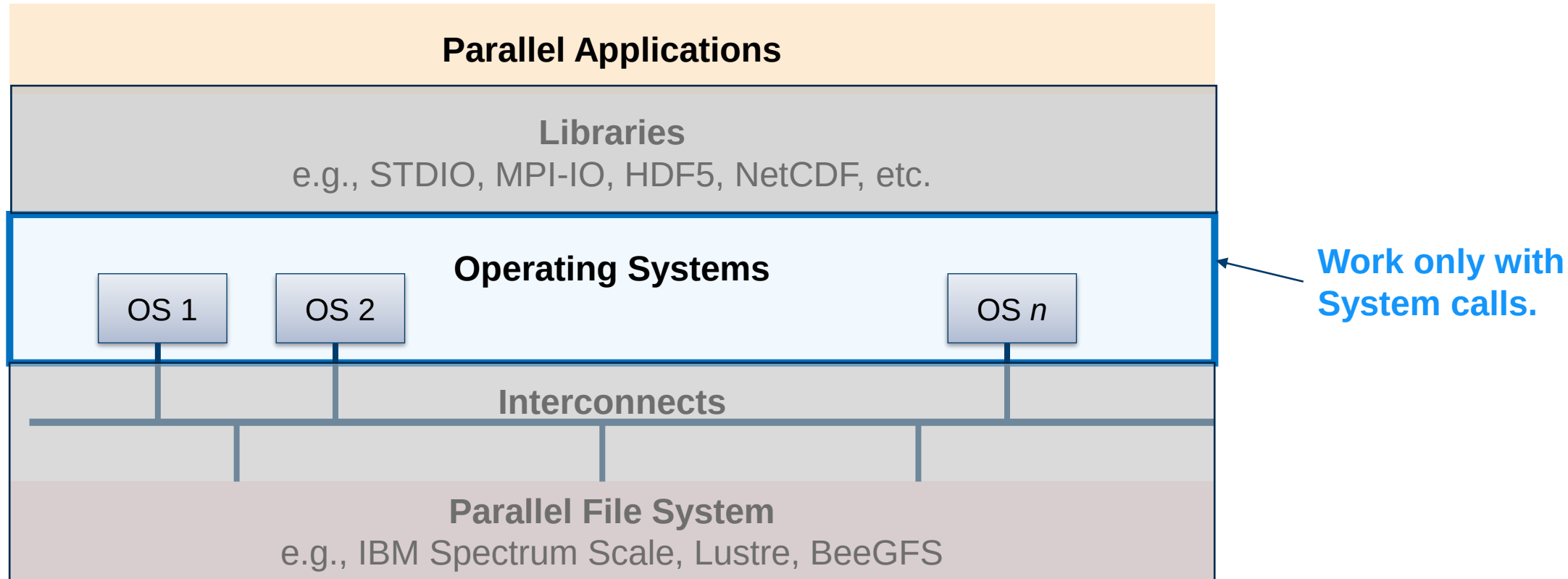
The Problem:

- How to include I/O in LAAB reports?
- Investigate the use of DFG method to **synthesize** the large amounts of I/O performance data.

WHICH I/O DATA TO USE?



WHICH I/O DATA TO USE?



TRACING WITH STRACE

Basic Usage:

```
strace [COMMAND]
```

Example:

```
$ strace ls
```

```
execve("/usr/bin/ls", ["ls"], 0x7ffd9ef46ac0 /* 36 vars */) = 0
brk(NULL)                               = 0x56490ef01000
arch_prctl(0x3001 /* ARCH_??? */, 0x7ffc49b7b440) = -1 EINVAL (Invalid argument)
mmap(NULL, 8192, PROT_READ|PROT_WRITE, MAP_PRIVATE|MAP_ANONYMOUS, -1, 0) = 0x7f9f2c1d8000
access("/etc/ld.so.preload", R_OK)      = -1 ENOENT (No such file or directory)
openat(AT_FDCWD, "/etc/ld.so.cache", O_RDONLY|O_CLOEXEC) = 3
newfstatat(3, "", {st_mode=S_IFREG|0644, st_size=38711, ...}, AT_EMPTY_PATH) = 0
mmap(NULL, 38711, PROT_READ, MAP_PRIVATE, 3, 0) = 0x7f9f2c1ce000
close(3)                                = 0
openat(AT_FDCWD, "/lib/x86_64-linux-gnu/libselinux.so.1", O_RDONLY|O_CLOEXEC) = 3
read(3, "\177ELF\2\1\1\0\0\0\0\0\0\0\0\3\0>\0\1\0\0\0\0\0\0\0\0\0\0...", 832) = 832
```

TRACING WITH STRACE

Example:

```
strace -f -tt -T -y -e read,write ls
```

pid	Timestamp	Sys Call	The file path	Bytes request	Transfer size	Duration
9054	08:55:54.153994	read(3	/usr/lib/x86_64-linux-gnu/libselinux.so.1	832	832	<0.000203>
9054	08:55:54.156640	read(3	/usr/lib/x86_64-linux-gnu/libc.so.6	832	832	<0.000079>
9054	08:55:54.159294	read(3	/usr/lib/x86_64-linux-gnu/libpcre2-8.so.0.10.4	832	832	<0.000087>
9054	08:55:54.162874	read(3	/proc/filesystems	1024	478	<0.000052>
9054	08:55:54.163049	read(3	/proc/filesystems	1024	0	<0.000040>
9054	08:55:54.163560	read(3	/etc/locale.alias	4096	2996	<0.000041>
9054	08:55:54.163679	read(3	/etc/locale.alias	4096	0	<0.000044>
9054	08:55:54.176260	write(1	/dev/pts/7	50	50	<0.000111>

TRACING WITH STRACE

Example:

```
srun -n 3 strace -f -tt -T -y -e read,write -o $hostname_$.st ls
```



host_9042.st



host_9043.st



host_9044.st

pid	Timestamp	Sys Call	The file path	Bytes request	Transfer size	Duration
9054	08:55:54.153994	read(3</usr/lib/x86_64-linux-gnu/libselinux.so.1>, ..., 832)		832		<0.000203>
9054	08:55:54.156640	read(3</usr/lib/x86_64-linux-gnu/libc.so.6>, ..., 832)		832		<0.000079>
9054	08:55:54.159294	read(3</usr/lib/x86_64-linux-gnu/libpcre2-8.so.0.10.4>, ..., 832)		832		<0.000087>
9054	08:55:54.162874	read(3</proc/filesystems>, ..., 1024)		478		<0.000052>
9054	08:55:54.163049	read(3</proc/filesystems>, "", 1024)		0		<0.000040>
9054	08:55:54.163560	read(3</etc/locale.alias>, ..., 4096)		2996		<0.000041>
9054	08:55:54.163679	read(3</etc/locale.alias>, "", 4096)		0		<0.000044>
9054	08:55:54.176260	write(1</dev/pts/7>, ..., 50)		50		<0.000111>

Trace file: host_9042.st

THE CHALLENGE

	pid	call	start	duration	bytes	fs	case	end
10	22085	read	1900-01-01 18:54:16.207116	0.000015	832	/p/software/fs/jusuf/stages/2024/software/HDF5...	st.jsfc134.22051.log	1900-01-01 18:54:16.207131
33	22085	read	1900-01-01 18:54:16.211619	0.000017	832	/p/software/fs/jusuf/stages/2024/software/psmp...	st.jsfc134.22051.log	1900-01-01 18:54:16.211636
221	22085	read	1900-01-01 18:54:16.246555	0.000008	832	/usr/lib64/libc.so.6	st.jsfc134.22051.log	1900-01-01 18:54:16.246563
231	22085	read	1900-01-01 18:54:16.247709	0.000015	832	/p/software/fs/jusuf/stages/2024/software/IME/...	st.jsfc134.22051.log	1900-01-01 18:54:16.247724
235	22085	read	1900-01-01 18:54:16.248466	0.000016	832	/p/software/fs/jusuf/stages/2024/software/Szip...	st.jsfc134.22051.log	1900-01-01 18:54:16.248482

⋮

Challenge: How do you extract useful information from large amounts of information in the system call traces?

THE SYNTHESIS METHOD

Idea:

- Map each row to a string that helps answer your question. We call this string “**Activity**”.
- Apply grouping based on activities and **compute statistics**.
- Identify the **directly-follows relation** between the activities to build a **Directly-Follows-Graph (DFG)**.

pid	call	start	duration	bytes	fs	<u>Activity</u>
22085	read	1900-01-01 18:54:16.207116	0.000015	832	/p/software/fs/jusuf/stages/2024/software/HDF5...	→ read+/p/software
22085	read	1900-01-01 18:54:16.211619	0.000017	832	/p/software/fs/jusuf/stages/2024/software/psmp...	→ read+/p/software
22085	read	1900-01-01 18:54:16.246555	0.000008	832	/usr/lib64/libc.so.6	→ read+/usr/lib64

THE SYNTHESIS METHOD

pid	call	start	duration	bytes	fs	Activity
22085	read	1900-01-01 18:54:16.207116	0.000015	832	/p/software/fs/jusuf/stages/2024/software/HDF5...	read+/p/software
22085	read	1900-01-01 18:54:16.211619	0.000017	832	/p/software/fs/jusuf/stages/2024/software/psmp...	read+/p/software
22085	read	1900-01-01 18:54:16.246555	0.000008	832	/usr/lib64/libc.so.6	read+/usr/lib64

- This data is can be formalized as an **event-log** in **Process Mining**.
- Process mining introduces **scalable techniques to translate event logs into** different types of dependency graphs, including **Directly-Follows Graph**.
- Ref: W. M. P. Van Der Aalst, “Foundations of process discovery,” in Process Mining Handbook, DOI: https://doi.org/10.1007/978-3-031-08848-3_2

THE SYNTHESIS METHOD



P0.strace.log



Activity
read+\$SOFTWARE
read+\$SOFTWARE
write+\$PROJECT



P1.strace.log



Activity
read+\$SOFTWARE
write+\$PROJECT
write+\$SCRATCH

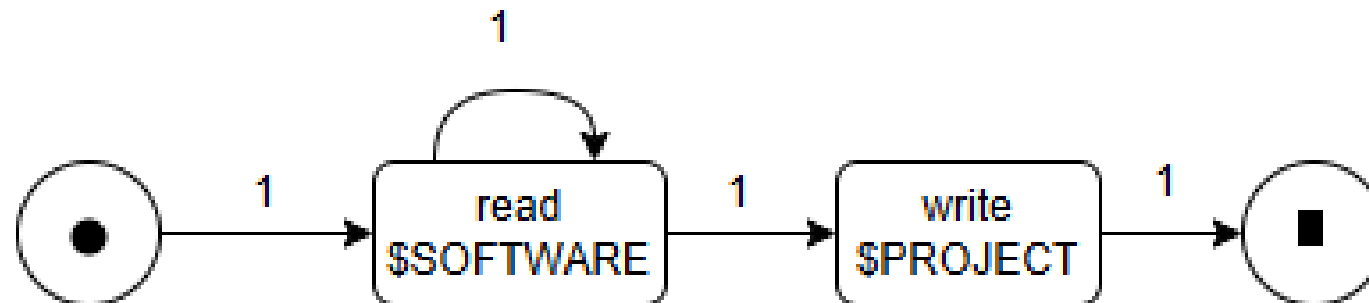
THE SYNTHESIS METHOD

P0

Activity
read+\$SOFTWARE
read+\$SOFTWARE
write+\$PROJECT

P1

Activity
read+\$SOFTWARE
read+\$PROJECT
write+\$PROJECT



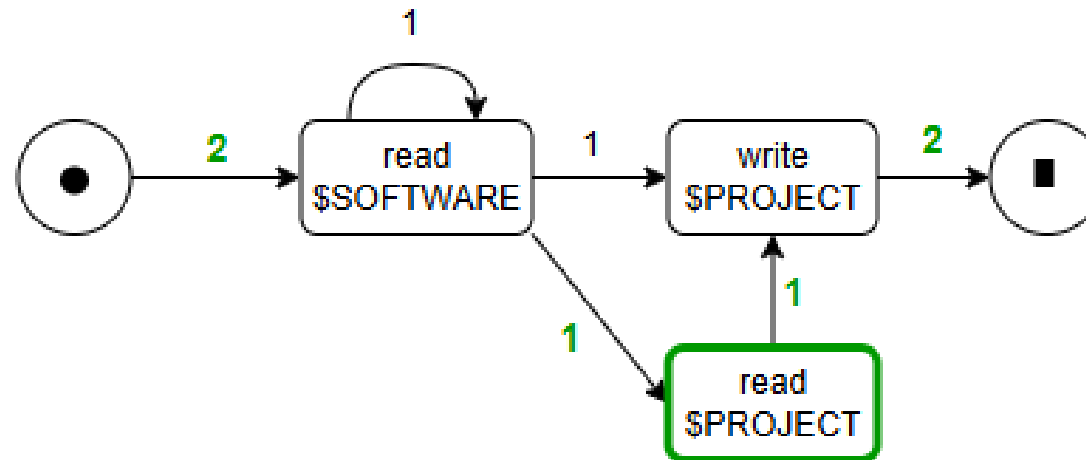
THE SYNTHESIS METHOD

P0

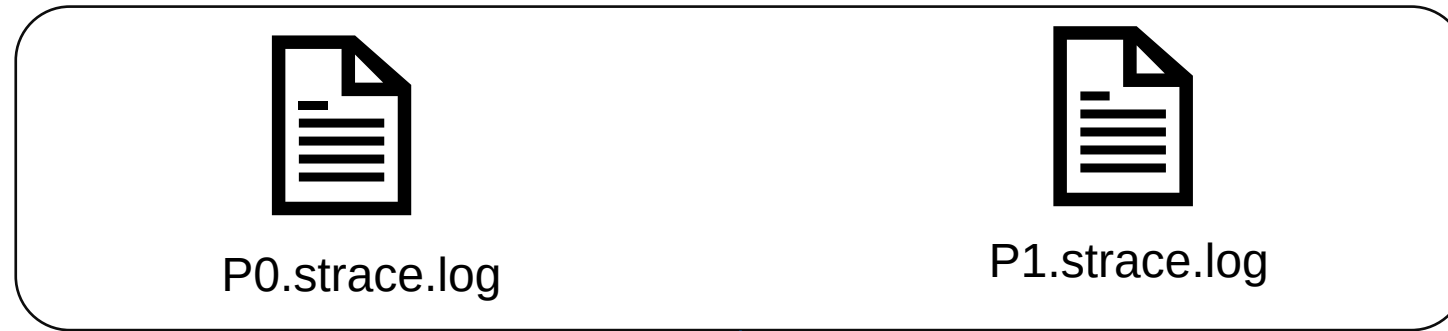
Activity
read+\$SOFTWARE
read+\$SOFTWARE
write+\$PROJECT

P1

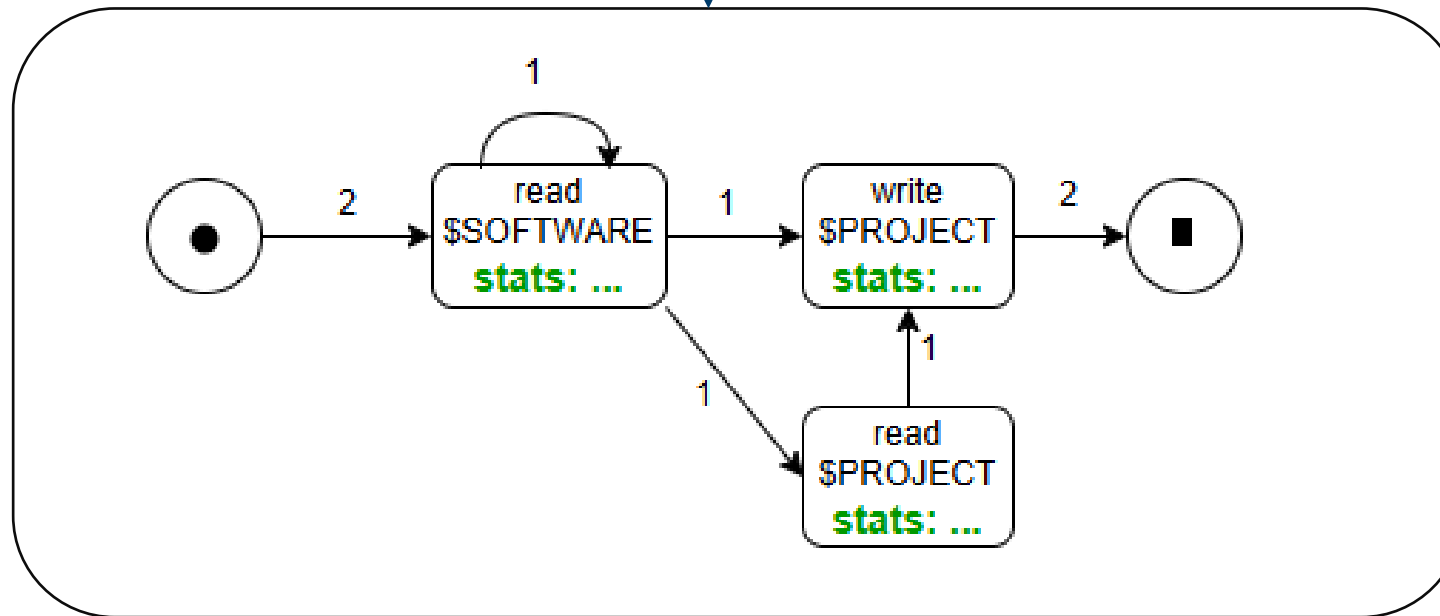
Activity
read+\$SOFTWARE
read+\$PROJECT
write+\$PROJECT



THE SYNTHESIS METHOD

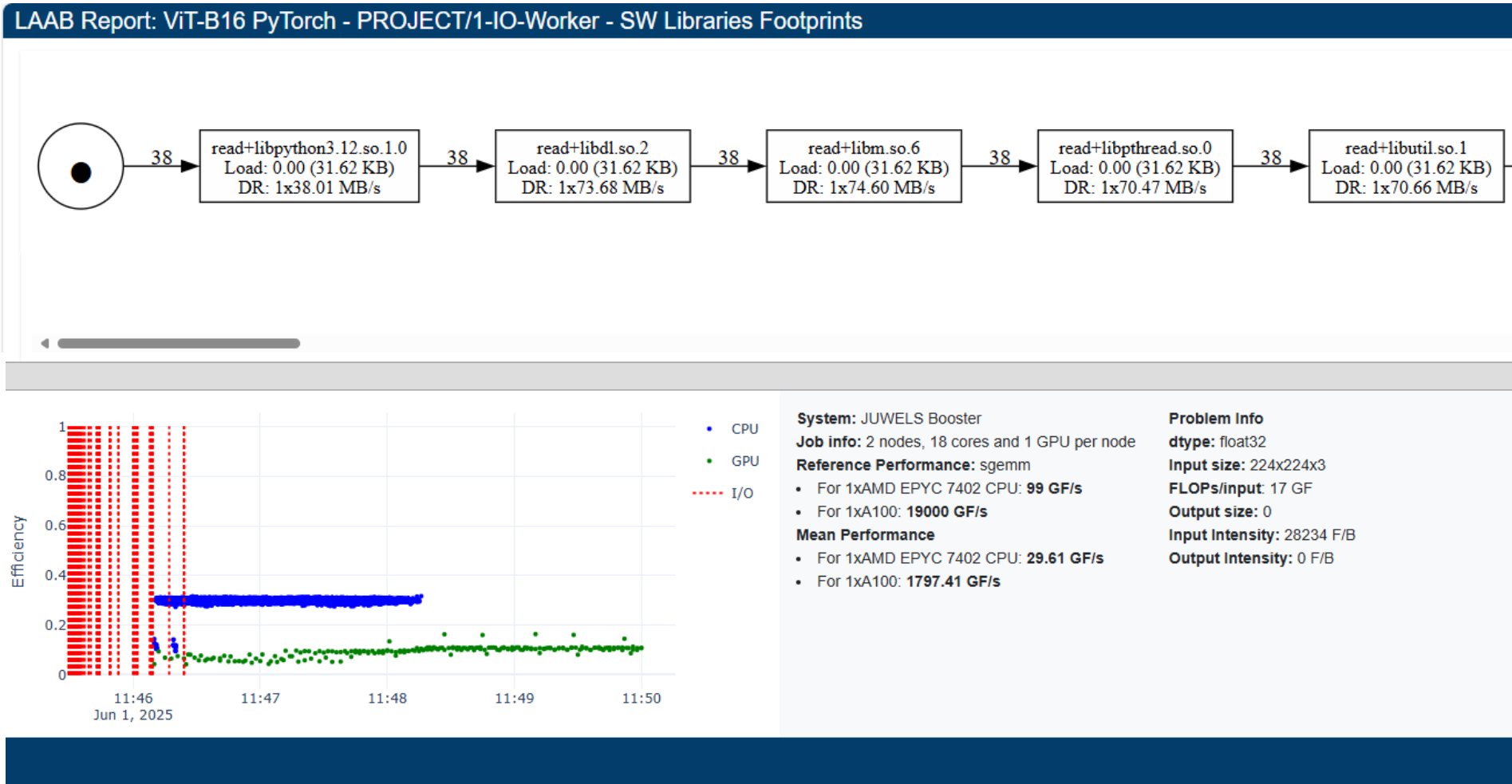


Logs from multiple processes are transformed into one DFG.



DEMO

SNAPSHOT OF LAAB REPORT WITH I/O



THE IMPLEMENTATION: STRACE INSPECTOR

- One log file is generated per node used.
- The parsing of log files and mapping to activities are done in parallel (*in v1.1.0*).
- The construction of DFG requires one pass through the activity log - $O(n)$, where n is the number of lines in the filtered event log after mapping.
- The complexity of rendering the DFG is $O(m^2)$, where m is the number activities. For all intents and purposes, m should be small.

Source code: https://gitlab.jsc.fz-juelich.de/st-inspector/st_inspector

Ref: A. Sankaran, I. Zhukov, W. Frings and P. Bientinesi, "Inspection of I/O Operations from System Call Traces using Directly-Follows-Graph," *SC24-W: Workshops of the International Conference for High Performance Computing, Networking, Storage and Analysis*, Atlanta, GA, USA, 2024, pp. 1562-1575, doi: 10.1109/SCW63240.2024.00196

Acknowledgements

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